

Theoretical Frameworks for Estimating Internal Combustion Engine Power

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ABSTRACT

This review examines the principal theoretical routes used to estimate engine power without relying exclusively on full-scale dynamometer testing. The analysis spans ideal cycle formulations, zero-dimensional and quasi-dimensional combustion models, one-dimensional gas-exchange simulations, high-fidelity CFD, and emerging data-driven surrogates. Particular attention is given to how heat release, in-cylinder pressure evolution, volumetric efficiency, friction, pumping work, and fuel properties influence the prediction of indicated and brake output. Representative figures are used to compare modeling hierarchies, visualize fuel-energy partitioning, track pressure and heat-release phasing, map parameter sensitivity, and illustrate the dependence of brake power on engine speed and mean effective pressure. The review shows that low-order thermodynamic methods remain effective for screening and preliminary design, whereas combustion-resolved and CFD-based approaches are better suited to calibration, abnormal-combustion assessment, and fuel-flexibility studies. Machine-learning models can accelerate prediction, but their reliability improves when they are anchored to physics-based constraints. Overall, the most appropriate framework depends on the intended application, the level of fidelity required, the availability of input data, and the acceptable computational cost.

1. Introduction

The power delivered by an internal combustion engine remains one of the most important indicators of performance in transportation and stationary energy systems. Estimating that output with confidence is essential for engine sizing, efficiency analysis, calibration, emissions control, and design optimization. Although dynamometer measurements remain indispensable, theoretical prediction has become equally important because it allows performance to be explored across wide operating envelopes before expensive prototypes are built or tested.

The first layer of this predictive landscape is rooted in thermodynamic cycle analysis. Idealized Otto, Diesel, and Dual cycles provide compact analytical descriptions of how compression ratio, heat-addition mode, and specific-heat ratio influence thermal efficiency and work output. Even though these cycles do not capture the full complexity of practical engines, they remain useful because they establish physical bounds and clarify the dominant trends that govern power generation.

A more direct bridge between theory and measurable engine output is provided by in-cylinder pressure analysis. Quantities such as indicated mean effective pressure (IMEP), brake mean effective pressure (BMEP), and apparent heat-release rate connect combustion phasing to useful work. Pressure-based methods therefore occupy a central role in engine diagnostics, model calibration, and the interpretation of combustion

quality under both conventional and advanced operating strategies.

As computational capability has advanced, theoretical power estimation has expanded from simplified cycle models to zero-dimensional control-volume formulations, one-dimensional gas-exchange simulations, quasi-dimensional flame-propagation models, and full CFD calculations. These approaches allow the effects of valve timing, flow structures, turbulence, wall heat transfer, and fuel chemistry to be incorporated with progressively higher fidelity.

More recently, data-driven techniques have entered the field as complementary rather than purely substitute tools. Neural networks, Gaussian-process models, and other machine-learning methods can approximate engine behavior rapidly once trained, making them attractive for optimization and real-time applications. Their usefulness, however, depends strongly on the quality of the training data and on the degree to which physical constraints are retained.

Because no single framework is universally optimal, model choice must be aligned with purpose. Concept screening may justify ideal or zero-dimensional methods, whereas calibration, knock analysis, or alternative-fuel assessment may require multi-zone combustion models or CFD. The central objective of this paper is therefore to review the major theoretical approaches used to quantify engine power, clarify their governing assumptions, and discuss where each method is most effective.

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Nomenclature

Abbreviation

ICE – Internal Combustion Engine
 IMEP – Indicated Mean Effective Pressure
 BMEP – Brake Mean Effective Pressure
 CFD – Computational Fluid Dynamics
 HRR – Heat Release Rate
 EVC – Exhaust Valve Closing
 IVO – Intake Valve Opening
 CA50 – Crank Angle of 50% Heat Release
 WOT – Wide Open Throttle
 TDC – Top Dead Center

Symbol

P – Pressure (Pa)
 T – Temperature (K)
 V – Volume (m³)

2. Methodology

Theoretical quantification of engine power is built on a hierarchy of models that convert fuel energy into predicted indicated or brake output. The methodological pathway usually begins with idealized thermodynamic cycles and progressively adds real-gas effects, finite-rate combustion, gas exchange, heat transfer, and mechanical losses until the required predictive fidelity is reached.

For spark-ignition and compression-ignition engines, the Otto, Diesel, and Dual cycles remain the canonical starting point. Under the ideal-gas assumption, their thermal efficiencies are derived from the first law for closed systems and from the sequence of compression, heat-addition, expansion, and rejection processes. For example, the Otto-cycle efficiency is written as $\eta = 1 - (1/r^{(\gamma-1)})$, where r is the compression ratio and γ is the specific-heat ratio. The net work per cycle is represented by the area enclosed on the pressure-volume path.

To move beyond ideal behavior, theoretical models introduce variable specific heats, finite combustion duration, and measured or prescribed pressure traces. A common representation of combustion phasing is the Wiebe function, which approximates the rate of heat release as a function of crank angle. In that setting, IMEP is evaluated from the cycle integral $IMEP = (\oint PdV)/V_d$, and indicated power is then estimated from engine displacement, speed, and stroke configuration.

Brake output is obtained after subtracting the losses that separate indicated work from shaft work. These losses include friction, pumping, and accessory consumption, and they are often expressed through brake mean effective pressure (BMEP) and friction mean effective pressure (FMEP). Empirical forms such as Chen-Flynn-type relations or engine-specific friction correlations are frequently used when detailed tribological models are unavailable.

Volumetric efficiency is another critical element because charge induction directly limits the amount of chemical energy available for conversion. Its prediction depends on intake pressure, temperature, valve timing, runner geometry, boosting strategy, and throttling. For this reason, many engine models couple thermodynamic calculations with one-dimensional gas-exchange formulations or with experimentally informed intake and exhaust boundary conditions.

Zero-dimensional control-volume models improve fidelity by solving pressure and temperature histories across crank angle. A common formulation expresses the pressure evolution as $dP/d\theta = (\gamma - 1)/V \times dQ/d\theta - \gamma P/V \times dV/d\theta$, where $dQ/d\theta$ represents the net heat-release term and $dV/d\theta$ is obtained from slider-crank kinematics. These models are computationally efficient and are widely used for parametric studies, cycle analysis, and preliminary calibration.

Higher-order approaches extend this description by separating burned and unburned zones, resolving flame propagation, and incorporating turbulence-chemistry interaction. Quasi-dimensional and multi-zone models track mass fractions, combustion duration, and inter-zone heat transfer, offering improved estimates of combustion phasing and peak pressure. When detailed fuel chemistry is required, reduced or detailed kinetic mechanisms may be integrated through packages such as

Cantera or CHEMKIN.

The three summary tables retained in this manuscript serve complementary purposes. Table 1 lists the governing assumptions associated with the idealized cycles, Table 2 provides representative parameters for a typical spark-ignition engine, and Table 3 compares major modeling strategies in terms of complexity, data burden, and expected accuracy.

Table 1. Governing Equations for Theoretical Engine Cycles

Cycle Type	Key Assumptions
Otto	Instantaneous combustion, ideal gas, no heat loss
Diesel	Constant pressure combustion, no losses
Dual	Finite duration combustion

Table 2. Typical Parameters for SI Engine Model

Parameter	Value	Unit
Compression Ratio (r)	10:1	-
Displacement Volume (V_d)	2.0	L
Specific Heat Ratio (γ)	1.35	-
Peak Pressure (P_{max})	5.5	MPa
Engine Speed (N)	3000	rpm

Table 3. Model Comparison for Engine Power Prediction

Model Type	Input Requirements	Complexity	Accuracy	Application Stage
Air-standard cycle	r, γ	Low	Low	Preliminary design
Zero-D thermodynamic	$V(\theta), Q(\theta), \gamma(T)$	Medium	Moderate	Concept evaluation
CFD with kinetics	Full geometry, turbulence model, fuel mechanism	High	High	Detailed simulation

To represent heat losses, many theoretical frameworks employ wall heat-transfer correlations such as the Woschni relation, while valve mass flow is estimated using discharge-coefficient and compressible-flow formulations. The resulting cycle calculations are then validated against in-cylinder pressure measurements, chassis or engine dynamometer data, and, when available, combustion-phasing indicators or such as CA50 or apparent heat-release trends.

Modern methodological practice increasingly adds uncertainty quantification and surrogate modeling to the traditional workflow. Sensitivity studies on compression ratio, ignition timing, fuel properties, and intake pressure help identify the variables that dominate prediction error, while machine-learning models can be trained as fast-response surrogates for optimization or control.

Taken together, these methodological layers provide a structured route from physically transparent screening tools to high-fidelity predictive environments. The appropriate level of detail depends on whether the task is conceptual design, calibration support, abnormal-combustion assessment, alternative-fuel evaluation, or real-time estimation.

3. Results

Applying these theoretical frameworks reveals that engine-power estimation is not a single calculation but a linked sequence of physical interpretations. Figure 1 summarizes that sequence by connecting primary inputs, intermediate model layers, and final performance outputs. The figure emphasizes that useful power prediction depends not only on the combustion model itself but also on how heat release, gas exchange, friction, and thermal losses are represented across the workflow.

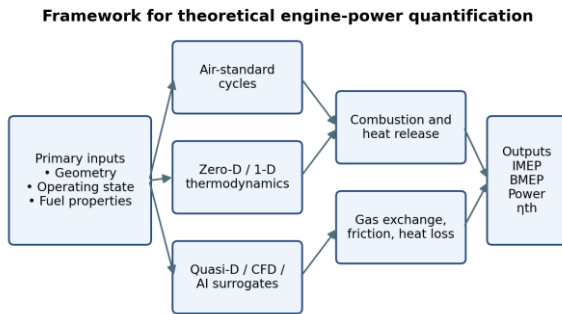


Fig. 1. Framework linking model inputs, modeling layers, and engine-power outputs.

The model hierarchy can also be compared on a multi-criteria basis. Figure 2 presents a radar-style assessment of common approaches, showing how air-standard cycles, zero-dimensional models, quasi-dimensional simulations, CFD, and hybrid AI tools differ in accuracy, interpretability, data demand, computational speed, transient capability, and calibration burden. The comparison makes clear that no framework is dominant in every category; rather, each occupies a different part of the fidelity-cost landscape.

From this perspective, low-order thermodynamic methods remain attractive because they are physically transparent and fast, whereas CFD provides the richest spatial detail at the expense of model preparation time and computational cost. Hybrid AI models occupy an intermediate position: they can deliver rapid predictions, but their robustness depends on how well the training dataset spans the operating domain and whether the surrogate respects known physical limits.

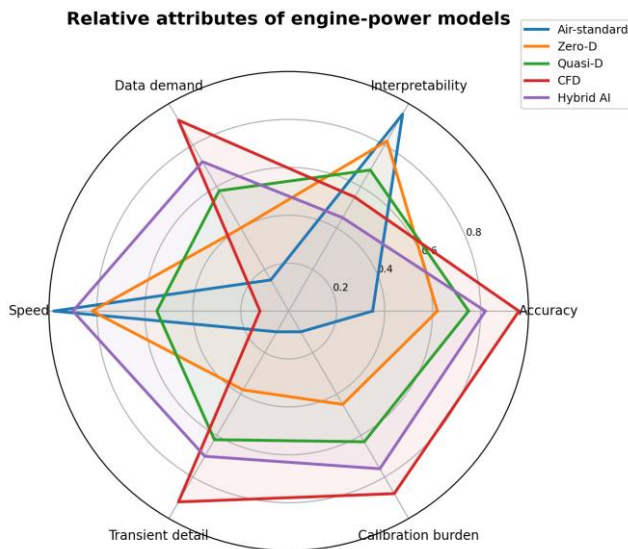


Fig. 2. Multi-criteria comparison of common engine-power modeling approaches.

A representative energy allocation is shown in Figure 3 using a stacked-bar format rather than a circular breakdown. The visualization highlights that only a fraction of the fuel lower-heating value emerges as brake work, while the remainder is redistributed to cooling losses, exhaust enthalpy, friction, pumping, and accessory demands. For

theoretical power estimation, this partition is important because even accurate combustion modeling can overpredict shaft output when these secondary losses are oversimplified.

Figure 4 pairs a typical cylinder-pressure trace with apparent heat-release phasing over crank angle. This combined representation is especially useful because it links the rise in pressure to the temporal distribution of combustion. The pressure peak appears shortly after top dead center, while the heat-release profile captures the onset, concentration, and decay of chemical energy liberation. Such phasing relationships are central to the calculation of IMEP and to the interpretation of knock tendency, combustion noise, and cycle efficiency.

The influence of major input variables is summarized in Figure 5 through a sensitivity heatmap. Compression ratio, spark timing, intake pressure, equivalence ratio, burn duration, and wall temperature do not affect all outputs equally. The figure shows, for example, that compression ratio and intake pressure exert strong positive influence on IMEP and brake power, while prolonged burn duration tends to reduce both predicted work output and efficiency. A sensitivity view of this type is useful when selecting calibration levers or screening the robustness of a theoretical model.

Brake output can also be visualized more clearly as a family of speed-power envelopes than as a three-dimensional response surface. Figure 6 therefore presents brake-power curves for several IMEP levels across engine speed. The line families show that higher mean effective pressure lifts the entire power envelope, whereas the shape of the curve remains constrained by the interaction of speed, filling, and mechanical losses. This format is often easier to interpret during design and calibration because it directly communicates the operating space available to the engine.

Beyond the figures, the theoretical results reinforce the role of geometry and combustion phasing in defining power capability. Increasing compression ratio generally raises thermal efficiency, but the associated gains must be weighed against higher knock propensity, greater mechanical loading, and more demanding fuel requirements. Similarly, faster combustion can improve IMEP by shifting the main heat-release period closer to the optimum crank-angle window, yet excessively rapid pressure rise may compromise durability and noise behavior.

Forced induction and fuel selection further modify the prediction landscape. Boosted operation increases trapped mass and generally raises power density, but it also alters intake temperature, exhaust back pressure, and the importance of intercooling. Alternative fuels change laminar flame speed, ignition delay, heating value, and autoignition characteristics, which means that a model calibrated for gasoline may not remain reliable when applied to methanol, ethanol, hydrogen, or gaseous fuels without revised sub-models.

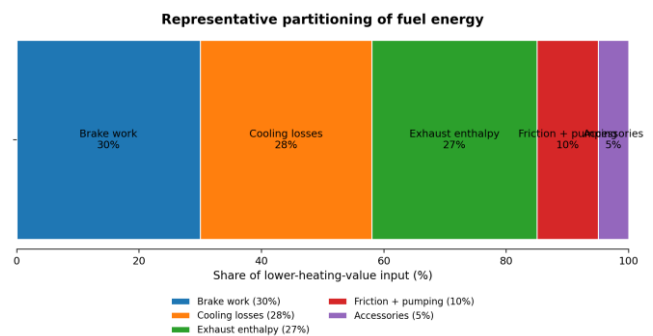


Fig. 3. Representative partitioning of fuel energy into useful work and major loss channels.

The rise of hybrid modeling strategies has broadened the practical usefulness of theoretical tools. Physics-based solvers can now be coupled with neural networks, Gaussian-process regressors, or reduced-order surrogates to accelerate repeated evaluation during optimization. These combinations are particularly valuable when a full CFD or multi-zone solution is too expensive to run inside an iterative design loop.

Validation nevertheless remains essential. Pressure transducers, dynamometer measurements, and combustion-phasing indicators continue to provide the reference against which theoretical predictions are judged. Discrepancies typically point to uncertainties in heat-transfer

treatment, friction estimation, trapped-mass prediction, or combustion-duration modeling rather than to a single isolated source of error.

Overall, the results indicate that theoretical power quantification should be approached as a layered decision problem. The most efficient framework is not the most detailed one, but the one that reproduces the dominant physics of the target problem with an acceptable computational burden and a transparent set of assumptions.

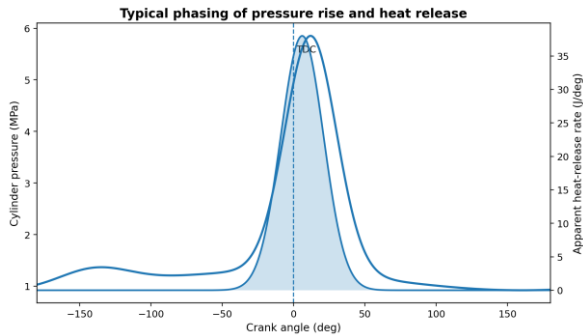


Fig. 4. Typical cylinder-pressure evolution and apparent heat-release phasing over crank angle.

The figures and interpretations collected in this section therefore support a consistent conclusion: engine-power estimation improves when thermodynamic, combustion, flow, and loss models are treated as mutually coupled elements rather than as isolated sub-calculations.

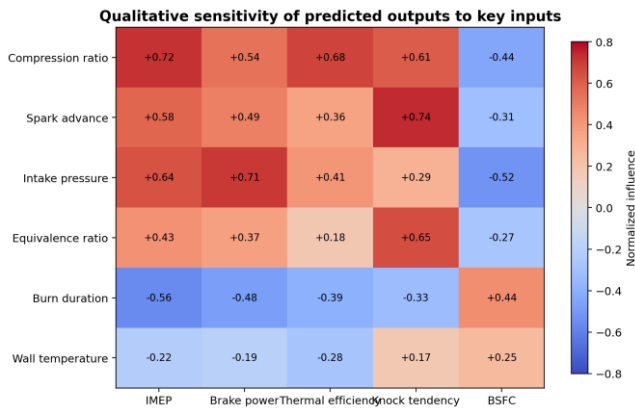


Fig. 5. Qualitative sensitivity of predicted outputs to key engine and operating inputs.

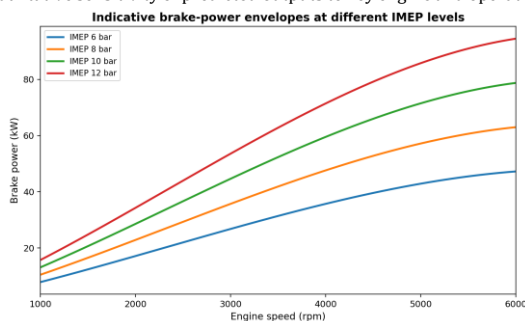


Fig. 6. Indicative brake-power envelopes across engine speed for different IMEP levels.

4. Discussion

The revised results underline a central principle in engine modeling: predictive value increases when model structure matches the engineering question being asked. A low-order formulation may be entirely sufficient for compression-ratio screening or preliminary efficiency trends, but it will not resolve localized flow structures, abnormal combustion, or transient torque response with the fidelity needed for advanced development tasks.

Ideal-cycle analysis remains useful because it exposes the first-order

thermodynamic logic of engine operation with very little computational cost. Its weakness is not that it is incorrect, but that it omits the mechanisms that separate conceptual work output from real brake power, including finite-rate combustion, wall heat transfer, gas exchange, and friction. Accordingly, these models should be interpreted as bounding tools rather than as standalone predictors of production-level performance.

Zero-dimensional and one-dimensional frameworks offer a more practical balance between cost and realism. They preserve direct physical meaning, accommodate pressure-trace analysis, and can be calibrated with manageable experimental input. However, they still compress spatially distributed processes into lumped representations, so their reliability depends heavily on the selected heat-release law, trapped-mass estimate, and wall-loss correlation.

Quasi-dimensional and CFD-based approaches address many of these limitations by resolving flame development, charge motion, and geometry-sensitive flow behavior in greater detail. Their advantage becomes especially clear when the task involves knock assessment, injector or spark-plug placement, high-EGR operation, or the transition to unfamiliar fuels. The trade-off is that these models demand careful meshing, robust boundary conditions, and substantial validation effort before their higher apparent fidelity can be trusted.

The sensitivity map developed in the results section also reinforces the need for disciplined parameter selection. Compression ratio, spark timing, intake pressure, and burn duration do not simply alter predicted power by fixed increments; they interact nonlinearly with one another and with fuel chemistry. This means that calibration strategies based on single-parameter sweeps can be informative, but they may still miss coupled effects that become important near operating limits.

Fuel dependence remains one of the most consequential sources of model uncertainty. Alternative fuels modify flame speed, stoichiometric requirements, ignition delay, and thermal loading, so the same theoretical framework may need different sub-model constants or even a different combustion description when the fuel is changed. This is particularly relevant in current research on low-carbon and renewable fuels, where predictive flexibility is increasingly important.

Engine architecture introduces another layer of variability. Bore-to-stroke ratio, cylinder number, valve strategy, and boosting configuration shape both volumetric efficiency and combustion quality. A model that ignores these geometric influences may still reproduce broad trends, but it will struggle to explain why two engines with similar displacement can exhibit very different power-density and efficiency characteristics.

Loss modeling deserves equal attention. Friction, pumping work, accessory demand, and thermal rejection determine the gap between indicated and brake output. Because these losses are often treated with empirical sub-models, they can become the dominant source of error once the combustion calculation itself has been improved. For that reason, better shaft-power prediction is often achieved not by making combustion models more elaborate, but by improving the representation of parasitic losses.

Transient operation remains one of the hardest regimes for purely theoretical prediction. Many review-level models implicitly assume quasi-steady behavior, while real engines experience rapid load, speed, and thermal excursions. Capturing these events requires time-resolved coupling between combustion, gas exchange, actuator dynamics, and control logic, which is why co-simulation and reduced-order surrogates are increasingly important in modern workflows.

Model credibility ultimately depends on validation. Even the most sophisticated solver can generate misleading outputs if it is insufficiently constrained by pressure data, torque measurements, or uncertainty analysis. Uncertainty quantification is therefore not a secondary add-on; it is part of the interpretive framework that determines whether a prediction is merely plausible or genuinely decision-ready.

The growing use of machine learning should be interpreted in this same context. Data-driven models are powerful because they can approximate highly nonlinear behavior at very low run time, but they are vulnerable to extrapolation error and hidden bias in the training data. Their strongest role is usually as a surrogate wrapped around a physics-based backbone rather than as an unconstrained black-box replacement.

These modeling choices also matter for regulation and industrial deployment. Virtual calibration, pre-certification screening, and

powertrain optimization increasingly depend on theoretical tools capable of reproducing performance across standardized test cycles without prohibitive testing effort. As emissions and efficiency standards tighten, the value of reliable predictive modeling continues to increase.

There is also a clear educational dimension. Well-constructed theoretical models help students and practicing engineers understand how thermodynamics, combustion, flow, and losses combine to determine engine output. The clarity of a simplified model, when used within its valid range, remains a major strength rather than a limitation.

Finally, the broader sustainability agenda is pushing theoretical methods beyond the standalone engine. Modern studies increasingly embed engine models inside hybrid powertrains, aftertreatment systems, lifecycle assessments, and energy-management frameworks. That shift does not reduce the relevance of power prediction; instead, it places engine-power estimation inside a larger systems context in which efficiency, emissions, controllability, and carbon intensity must be evaluated together.

In that sense, the future of engine-power quantification lies not in choosing between simple and complex methods as opposing camps, but in integrating them intelligently. Fast thermodynamic models, combustion-resolved simulations, uncertainty tools, and machine-learning surrogates each contribute different forms of value, and the most effective workflows are likely to combine them in a staged and physically consistent manner.

5. Conclusion

Theoretical estimation of engine power remains a foundational task in engine research, design, and calibration. Across the spectrum from idealized cycles to CFD and data-driven surrogates, the common objective is to transform operating inputs into reliable predictions of indicated and brake output while retaining a clear understanding of the underlying physics.

Ideal Otto, Diesel, and Dual cycles continue to provide essential first-order insight into the effect of compression ratio, heat-addition mode, and specific-heat ratio. Their simplicity makes them valuable for screening and interpretation, even though they do not directly represent the losses and rate-controlled processes that govern practical engines.

Zero-dimensional and one-dimensional methods extend this foundation by incorporating pressure evolution, heat release, volumetric efficiency, and empirically informed loss models. Because they preserve physical transparency while remaining computationally light, they are still among the most useful tools for parametric studies and early-stage development.

When higher fidelity is required, quasi-dimensional, multi-zone, and CFD frameworks provide deeper access to combustion phasing, turbulence interaction, heat transfer, and geometry-specific effects. These approaches are especially important for abnormal-combustion analysis, alternative-fuel studies, and detailed design refinement, although they require substantially greater setup effort and validation.

A key conclusion of this revision is that loss representation is as important as combustion representation. Accurate shaft-power estimation depends not only on the prediction of in-cylinder work, but also on credible treatment of friction, pumping, accessory demand, and thermal rejection.

The reviewed material also shows that parameter sensitivity is strongly nonuniform. Compression ratio, spark timing, intake pressure, and burn duration can exert large but interacting influences on IMEP, efficiency, and brake output. Consequently, robust model-based prediction benefits from sensitivity analysis rather than reliance on isolated parameter changes.

Machine-learning tools are now valuable additions to the model hierarchy, particularly when fast evaluation is required for optimization, calibration, or control. Their most reliable role, however, is as physics-guided surrogates rather than unconstrained replacements for mechanistic understanding.

Validation remains indispensable throughout this hierarchy. Whether the model is simple or highly resolved, pressure traces, dynamometer

data, and uncertainty assessment are required to establish confidence in the predicted power trends and absolute values.

Theoretical power modeling is also becoming more system-oriented. Contemporary applications increasingly link the engine to boosting devices, aftertreatment, electrified drivetrains, and sustainability metrics, which means that engine power must be interpreted within a broader performance and emissions framework.

Overall, no single method is universally superior. The most effective approach is the one that captures the dominant mechanisms of the target problem with the least unnecessary complexity and with assumptions that remain visible to the user.

Future progress will likely come from better integration across scales: transparent thermodynamic screening, combustion-resolved sub-models, uncertainty-aware calibration, and machine-learning acceleration working within one coherent workflow.

For that reason, theoretical engine-power quantification should be regarded not as a fixed method but as an evolving modeling ecosystem - one that remains central to efficient engine development, fuel evaluation, and the broader transition toward cleaner and more optimized propulsion systems.

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